The concordance between the different values in each row of Table III and the close agreement between most of the experimental and calculated values of Table IV show the general applicability of the assumed relationships and constants. The calculated bond energies rarely differ more than 2 or 3 kcal./mole from the experimental values. The larger differences for  $H_3As$ ,  $H_2Se$  and  $H_2Te$ are probably due to poor enthalpy data, based on experimental results published in 1888 and earlier. The discrepancies for the simple organic derivatives of sulfur and iodine may be due to error in the assumption that the C-H bond energy is strictly constant. Likewise, the calculation of the N-N bond energy in  $N_2H_4$  on the assumption that the N-H bond energy is the same as in NH<sub>3</sub> is probably unjustified (see Skinner<sup>6</sup>).

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# Atomic Radii. IV. Dependence of Interatomic Distance on Bond Energy<sup>1</sup>

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It is shown that most of the departures from strict additivity of radii in normal valence compounds can be attributed to variations in bond energy,  $D_{AB}$ . A set of "constant energy radii,"  $r_A^*$ , has been computed. The simple relationship,  $r_{AB} = r_A^* + r_B^* - \frac{1}{2} \log D_{AB}$ , yields interatomic distances which average within 0.02 Å. of the best experimental values. If experimental bond energies are not available, values computed from electronegativities and non-polar bond-energy contributions (see the preceding paper) can be used, with but little loss of accuracy.

#### Introduction

The hypothesis of constant additive atomic radii was introduced in 1920 by Bragg.<sup>2</sup> Shortly thereafter the writer showed<sup>3</sup> that the Lewis theory of valence was as applicable to crystals as to molecules and ions and pointed out<sup>4</sup> that the valence electron distributions so obtained enable one to predict, in many cases, whether or not constancy and additivity of radii should exist. Various causes of variability were considered in a qualitative manner. It was shown, nevertheless, that a reasonable degree of constancy and additivity exists in certain classes of structures, the essential requirement being that each atom being considered has a sufficiently similar environment in the different substances being compared. Sets of radii for several such classes were computed, the most extensive being a set of tetrahedral radii,5 computed from and for bonds joining atoms, each having a kernel charge +n, tetrahedrally to four others, each with a kernel charge of 8 - n. In 1934, Pauling and Huggins<sup>6</sup> revised and extended these sets of radii and added a set of normal valence radii, differing for only six elements from the tetrahedral radii (see Table I).

The writer has consistently pointed out that one should not expect close correspondence between the experimental interatomic distance and the sum of the appropriate radii from the standard set, if the environment of either or both of the atoms differs much from that of the corresponding atom in the class of substances from which the standard radii were derived. Such departures from additivity are, in fact, often found. They are useful in supplying evidence regarding the dependence of the bond length on various factors.

Many of the more marked departures from additivity have been interpreted<sup>7</sup> as resulting from differences in the "degree of double-bond character." On the other hand, Schomaker and Stevenson<sup>8</sup> attribute these departures to varying degrees of bond polarity. They have published a set of *non-polar radii* ( $r_{np,A}$ ) and proposed the following empirical equation for the calculation of singlebond distances from these radii and Pauling's electronegativities<sup>7,9</sup> ( $x_A$ )

$$r_{AB} - r_{np,A} + r_{np,B} - 0.09 |x_A - x_B|$$
 (1)

Although both of these explanations of departures from additivity seem reasonable and can be used to account for the observed distances in a considerable number of instances, Wells<sup>10</sup> has concluded that the sum total of available evidence is against the general applicability of either.

The present paper reports the results of an attempt to correlate interatomic distances with bond energies in a simple manner for single bonds in normal valence elements and compounds.

## Theoretical Background

It is theoretically reasonable and experimentally well established that, other things being equal, the greater the bond energy the shorter is the interatomic distance. The bond energy is minus the sum of the repulsion energy and the (negative) attraction energy, when the molecule is in its lowest energy state, *i.e.*, when the interatomic distance is  $r_{AB}$ 

$$D_{AB} = -E \text{ when } r = r_{AB} \tag{2}$$

$$E = E_{\rm rep} + E_{\rm att} \tag{3}$$

<sup>(1)</sup> This is a revision of portions of papers presented on Sept. 22, 1949, at the 116th Meeting of the American Chemical Society in Atlantic City and on Sept. 13, 1951, at the XIIth International Congress of Pure and Applied Chemistry in New York, N. Y. For the three previous papers in this series, see references 4, 5 and 6.

<sup>(2)</sup> W. L. Bragg. Phil. Mag., [6] 40, 169 (1920).

<sup>(3)</sup> M. L. Huggins, THIS JOURNAL, 44, 1841 (1922).

<sup>(4)</sup> M. L. Huggins, Phys. Rev., 19, 346 (1922).

<sup>(5)</sup> M. L. Huggins, ibid., 21, 205 (1923); 28, 1086 (1926).

<sup>(6)</sup> L. Pauling and M. L. Huggins, Z. Krist., **A87**, 205 (1934); quoted in ref. (7).

<sup>(7)</sup> L. Pauling, "The Nature of the Chemical Bond," Cornell University Press, Ithaca, N. Y., 1939.

<sup>(8)</sup> V. Schomaker and D. P. Stevenson, This Journal, 63, 37 (1941).

<sup>(9)</sup> L. Pauling. ibid., 54, 3570 (1932).

<sup>(10)</sup> A. F. Wells, J. Chem. Soc., 55 (1949).

				TABL	ЕI								
Atomic Radii													
	Hª	НÞ	Η¢	Hď	Ηe	С	Ν	0	F	Si	Р	s	Cl
H <sup>5</sup> 1926 Tetrahedral						0.77	0.70	0.65	0.61	1.14	1.08	1.02	0.97
P & H <sup>6</sup> 1934 Tetrahedral						.77	.70	.66	.64	1.17	1.10	1.04	. 99
P & H <sup>6</sup> 1934 Normal valence	0.375	0.28	0.28	0.28	0.28	.77	.70	. 66	. 64	1.17	1.10	1.04	. 99
S & S <sup>8</sup> 1941 Non-polar	.37	.37	.37	.37	.37	.77	.74	.74	.72	1.17	1.10	1.04	.99
H 1953 Non-polar $(r_{np,A})$	.38	. 36	.34	. 33	.32	.77	.75	.74	.72	1.15	1.11	1.04	1.00
H 1953 Constant energy $(r_{\rm A}^*)$	. 88	.86	.84	.83	.82	1.22	1.12	1.12	1.11	1.57	1.53	1.46	1.44
			Ge	As	Se	Br	Sn	Sb	Te	I			
H <sup>5</sup> 1926 Tetrah	edral		1.2	1 1.10	6 1.1	2 1.0	9 1.3	6 1.29	1.23	3 1.19	9		
P & H <sup>6</sup> 1934 Te	trahedra	1	1.2	2 1.18	8 1.1	4 1.1	1 1.4	0 1.36	3 1.32	2 1.2	8		
P & H <sup>6</sup> 1934 Normal valence			1.2	2 1.2	1 1.1	7 1.1	4 1.4	0 1.41	1.37	7 1.3	3		
S & S <sup>8</sup> 1941 Non-polar			1.2	2 1.2	1 1.1	7 1.1	4 1.4	0 1.41	1.37	7 1.3	3		
H 1953 Non-polar $(r_{np,A})$			1.2	1 1.2	4 1.1	7 1.1	4 1.4	2 1.48	5 1.41	1 1.3	5		
H 1953 Constant energy $(r_A^*)$			1.6	1 1.63	31.5	8 1.5	6 1.8	0 1.83	1.79	9 1.73	3	•	

<sup>a</sup> In H<sub>2</sub>. <sup>b</sup> In bonds with first row elements. <sup>c</sup> In bonds with second row elements. <sup>d</sup> In bonds with third row elements. \* In bonds with fourth row elements.

The repulsion energy, due primarily to overlapping of the electron clouds of the two atoms concerned, would be expected to vary with the interatomic distance in a manner depending only slightly on the nature and magnitude of the attractions between the atoms. This expectation has been tested and verified for alkali halide crystals by Huggins and Mayer,<sup>11,12</sup> using the exponential repulsion law of Born and Mayer<sup>13</sup>

$$E_{\rm rep} = E_{\rm rep}^* \exp\left[a(r_{\rm AB}^* - r)\right] \tag{4}$$

It was found that (with  $E^*_{rep}$  assigned an arbitrary value, the same for all compounds) the constant ain the exponential varies but little from compound to compound and also that, assuming it to be accurately the same in all cases, the constant energy distances, r<sup>\*</sup><sub>AB</sub>, can be additively computed from constant energy radii, r<sub>A</sub>, characteristic of the atoms concerned

$$r_{\rm AB}^* = r_{\rm A}^* + r_{\rm B}^* \tag{5}$$

These designations for  $r_{AB}^*$  and  $r_{A}^*$  arise from the fact that the former is the distance between atomic centers when the repulsion energy has the constant value  $D_{rep}^0$ .

A similar treatment<sup>14,15</sup> has been found satisfactory, at interatomic distances not far from the equilibrium values, for diatomic molecules. Following Morse,16 an exponential expression was also used for the attraction energy

$$E_{\text{att}} = E_{\text{att}}^{\text{e}} \exp\left[a'(r_{\text{e}} - r)\right] \tag{6}$$

The constants  $E_{att}^{e}$  and a' do not have the same values for different molecules or for the same molecule in different energy states. For molecules containing only electronegative atoms or hydrogen, a uniform value of a could again be used, and again the  $r_{AB}^*$  values computed were found to obey fairly well the additivity relationship (equation (5)).

On assuming equations (3), (4) and (6) and deducing the constants from band spectral data for diatomic molecules, equation (2) is found to be far from accurate. Nevertheless, we shall tentatively

assume, as an approximation, that all four of these equations (and also equation (5)) hold for single bonds in normal valence molecules containing only electronegative atoms and hydrogen, with the constants determined by experimental bond-energy and interatomic distance data. We thus have

$$D_{AB} = -E_{att}^{e} - E_{rep}^{*} \exp[a(r_{AB}^{*} - r_{e})]$$
(7)

From the equilibrium condition

$$dE/dr = 0 \text{ when } r = r_e \tag{8}$$

one can deduce

$$-E_{\rm att}^{\rm e} = \frac{a}{a'} E_{\rm rep}^{*} \exp\left[a(r_{\rm AB}^{*} - r_{\rm e})\right]$$
(9)

Combining equations (7) and (9), we have

$$D_{AB} = \left(\frac{a}{a'} - 1\right) E_{rep}^* \exp[a(r_{AB}^* - r_e)]$$
(10)

We shall assume, for our present purpose, that the first factor in parentheses in this equation is essentially constant. This is equivalent to assuming that the repulsion energy at equilibrium is proportional to the bond energy. The bandspectrum data for diatomic molecules give some justification for this assumption, as a rough approximation. It is less drastic than Morse's hypothesis,<sup>16</sup> that a = 2a'. Although essentially an *ad hoc* assumption, the data to be presented will testify as to its general validity. It is possible, nevertheless, that variability of this factor may, in some cases, not be negligible.

Since the value of  $E_{rep}^*$  is entirely arbitrary, we shall assume it to have such a value that

$$\left(\frac{a}{a'} - 1\right) E_{\rm rep}^* = 1 \text{ kcal./mole}$$
(11)

Then, replacing  $r_e$  by its approximate equivalent,  $r_{\rm AB}$ , we have

$$D_{AB} = \exp[a(r_{AB}^* - r_{AB})]$$
(12)

$$r_{\rm AB} = r_{\rm AB}^* - \frac{1}{a} \ln D_{\rm AB}$$
 (13)

This equation, combined with the additivity relation (equation (5)), has been tested by application to all available pertinent data. Complete sets of calculations have been made, in which ais taken equal to 4.00, 4.605 and 6.00  $\times$  10<sup>8</sup> cm.<sup>-1</sup>, with less extensive sets for some other values.

<sup>(11)</sup> M. L. Huggins and J. E. Mayer, J. Chem. Phys., 1, 643 (1933).
(12) M. L. Huggins, *ibid.*, 5, 143 (1937).

<sup>(13)</sup> M. Born and J. E. Mayer, Z. Physik, 75, 1 (1932).
(14) M. L. Huggins, J. Chem. Phys., 3, 473 (1935).
(15) M. J. Warding, 11, 14, 202 (1935).

<sup>(11)</sup> M. L. Huggins, J. Chem. 1 hys., 9, 413
(15) M. L. Huggins, *ibid.*, 4, 308 (1936).
(16) P. M. Morse, *Phys. Rev.*, 34, 57 (1929).

## TABLE II INTERATOMIC DISTANCES

Bond	rAB caled. from normal	$r_{AB}$ calcd. from $D_{np,A}$	Molecule	rAB calcd. from exp.	rab	Source or rAB
H_H	0.75	0 751	U.	0.751	0.740	(exp.)-
H-H H-C	1.07	1 119		0.701	1 004	3
11–C	1.07	1,110	C.H.	1.111	1.094	5 64
H-N	1 00	1 016	C2116	1 017	1.102	2
н-ц н-о	0.06	0.062	H.O	0.059	0.057	5
п-0 и Б	0.90	0.903		0.908	0.907	5
H-r U Si	0.94	0.902	nr Su	0.900	0.920	5
п-зі цр	1.47	1.401	DII DII	1,400	1,400	S'
п-г	1.40	1.420	FII3	1,428	1 424	5.
це	1 94	1 947	US	1 995	1,419	M <sup>2</sup>
	1.04	1.047	HC1	1.330	1.004	S'
H-CI	1.29	1.270		1.273	1.284	5
п-Ge	1.02	1.000		•	1.478	S
11 4 2	1 51	1 594	GenaCI	1 570	$1.52 \pm 0.01$	M.
H-AS	1.01	1.034	ASI 3	1.570	1.523	S', M'
п-се и р.	1.47	1.410	IID.	1.000	1.0	5. 0h
H-DI U Sm	1.44	1.410	UDI UDI	1.419	1.423 1.700 - 0.017	5 3.5k
	1.70	1.094			$1.700 \pm 0.015$	M.
H-90	1.71	1.729	SDH3		1.711	5
<u>и</u>	1 67	1 000	<b>Π</b> .	1 70	1.712	M
H-Ie	1.07	1.690	H <sub>2</sub> le	1.73	1 017	<b>c</b> h
	1.00	1.010	HI	1.623	1.017	S'
	1.04	1.007	$C_2H_6$	1.00	$1.55 \pm 0.03$	E
			Diamand	1 54	1.543	S" VOM
				1.04	1.541	XC <sup>m</sup>
ON	1 47	1 400	$C(CH_3)_4$	1 40	$1.54 \pm 0.02$	E
CIN	1.47	1.489	CH <sub>3</sub> NH <sub>2</sub>	1.48	1.48	5
				1 40	$1.47 \pm 0.01$	E'
			$C_2\Pi_5 N\Pi_2$	1.48	$1.47 \pm 0.02$	
			$(C\Pi_3)_2$ INIT	1.49	$1.47 \pm 0.02$	$\mathbf{E}^{l}$
			(CII) N		$1.40 \pm 0.03$	
			$(CH_3)_{3}$ IN		$1.47 \pm 0.01$	
<u> </u>	1 49	1 495			$1.48 \pm 0.01$	E $E^{l}$
<b>C</b> =0	1.40	1.400		1 49	$1.44 \pm 0.01$	E E
				1.42	$1.43 \pm 0.03$ 1.43 $\pm 0.05$	
					$1.43 \pm 0.03$	E F <sup>l</sup>
			CHONO		$1.44 \pm 0.03$	
C F	1.41	1 265	CF CF	1 955	$1.44 \pm 0.02$	
C-r	1.41	1.505		1.500	$1.30 \pm 0.02$	$E^{l}$
			CHr3		$1.30 \pm 0.03$	
					$1.34 \pm 0.02$	E
					1.049	5
			CH F.		1.002 1.20 $\pm$ 0.01	IVI CP
			$C11_{2}1_{2}$		$1.32 \pm 0.01$ 1.259 $\pm 0.001$	Mg
					$1.358 \pm 0.001$ 1.357 $\pm 0.017$	F <sup>r</sup>
			CH.F		1 308	Se
			CIIII		1.090 1.49 $\pm$ 0.09	
					$1.42 \pm 0.02$ 1.39 $\pm 0.02$	$\mathbf{E}^{l}$
					1.385	$M^*$
			CC1F <sub>2</sub>		1 323	$M^t$
			CCl <sub>2</sub> F <sub>2</sub>		$1.35 \pm 0.03$	$\mathbf{E}^{l}$
			CCl <sub>3</sub> F		$1.40 \pm 0.04$	$\mathbf{E}^{l}$
			-		$1.44 \pm 0.04$	$\mathbf{E}^{l} \bullet$
			CBrF3		1.321	$\mathbf{M}^{u}$
			-		$1.33 \pm 0.015$	$\mathbf{M}^{v}$
			CBr₃F		$1.44 \pm 0.06$	$\mathbf{E}^{l}$
			CIF <sub>3</sub>		$1.33 \pm 0.015$	M <sup>ν</sup>
			CHClF <sub>2</sub>		$1.36 \pm 0.03$	$\mathbf{E}^{l}$
			CHCl <sub>2</sub> F		$1.41 \pm 0.03$	$\mathbf{E}_{i}^{l}$
			CH <sub>2</sub> ClF		$1.40 \pm 0.03$	$\mathbf{E}^{l}$
Ç-Si	1.94	1.883	SiC	1.89	1.89	$\mathbf{X}\mathbf{C}^m$
			$Si(CH_3)_4$		$1.888 \pm 0.02$	$\mathbf{E}^{w}$

TABLE II (Continued)						
	rAB calcd.	rAB caled.	Molecule	TAB calcd.	*1B	Source
Bond	valence radii <sup>6</sup>	and $x_A^{17}$	crystal	$D_{\rm AB^{17}}$	(exp.)	$(exp.)^a$
			CH3SiF3		1.88	M
			$(CH_3)_2SiCl_2$		$1.83 \pm 0.06$	$\mathbf{E}_{,}^{l}$
C-P	1.87	1.865	$P(CH_3)_3$	<i>c</i> 00	$1.87 \pm 0.02$	$\mathbf{E}'_{\mathbf{D}'}$
C-S	1.81	1.812	$(CH_3)_2S$	1.83	$1.82 \pm 0.01$ 1.78 $\pm$ 0.02	E' E'
C - C1	1 76	1 754	$(CH_3)_2O_2$	1 740	$1.78 \pm 0.03$ 1.755 $\pm 0.005$	E F <sup>l</sup>
C CI	1.10	1.104	004	1.140	$1.760 \pm 0.000$ 1.765 ± 0.015	$E^{l}$
					1.761	$\mathbf{E}^{l}$
					$1.77 \pm 0.02$	$\mathbf{E}^{l}$
					$1.75\pm0.01$	XG <sup>y</sup>
			CHCl3	1.75	1.767	M
					$1.77 \pm 0.02$	E'
				1 75	1.81	XG
			$C\Pi_2 CI_2$	1.75	$1.77 \pm 0.02$	الال الال
			CH.Cl	1 75	$1.77 \pm 0.02$ 1.77 + 0.01	$E^{l}$
			011,01	1.10	$1.780 \pm 0.002$	$\mathbf{\tilde{M}}^{aa}$
					1.779	$\mathbf{M}^{ab}$
					1.7810	$\mathbf{M}^{ac}$
			CC1F3		1.765	$\mathbf{M}^{t}$
			$CCl_2F_2$		$1.74 \pm 0.03$	$\mathbf{E}'_{i}$
			CCl <sub>3</sub> F		$1.76 \pm 0.02$	E, .
			CHCLIF		$1.73 \pm 0.04$ 1.72 \dots 0.02	
			CH <sub>2</sub> CIF		$1.73 \pm 0.03$ 1.76 $\pm 0.02$	E F <sup>l</sup>
			CBr <sub>2</sub> Cl <sub>2</sub>		$1.75 \pm 0.02$	$E^{l}$
			CBrCl <sub>3</sub>		1.76	$\tilde{\mathbf{E}}^{l}$
			C(CH <sub>3</sub> ) <sub>8</sub> CH <sub>2</sub> C1		$1.74\pm0.03$	$E^{ad}$
			$Si(CH_3)_3CH_2C1$		$1.73\pm0.03$	$\mathbf{E}^{ad}$
C-Ge	1.99	1.939	Ge(CH <sub>3</sub> ) <sub>4</sub>		$1.98 \pm 0.03$	$\mathbf{E}_{,}^{l}$
C-As	1.98	1.983	As(CH <sub>3</sub> ) <sub>3</sub>		$1.98 \pm 0.02$	E'
C-Br	1.91	1.909	CBr <sub>4</sub>	1.908	$1.91 \pm 0.02$	E'
					$1.93 \pm 0.02$ 1.04 $\pm$ 0.02	면 파 <sup>1</sup>
					$1.942 \pm 0.02$ 1.942 \pm 0.003	$E^{l}$
			CHBr <sub>3</sub>	1.91	1.91	$\mathbf{E}^{l,as}$
					$1.930 \pm 0.003$	$\mathbf{M}^{af}$
			$CH_2Br_2$	1.91	$1.91 \pm 0.02$	$\mathbf{E}^{l}_{i}$
			CH₃Br	1.91	$1.91 \pm 0.06$	$\mathbf{E}^{t}$
			0.0.0		1.9391	$M^{ac}$
			CBrF <sub>3</sub>		1.936	M <sup>-</sup>
			CBrok		$1.91 \pm 0.02$	$\mathbf{E}^l$
			CBrCl		2.01 2.01	$\tilde{\mathbf{E}}^{l}$
			CBr <sub>2</sub> Cl <sub>2</sub>		1.93	$\mathbf{E}^{l}$
C-Sn	2.17	2.140	$Sn(CH_8)_4$		$2.18 \pm 0.03$	$\mathbf{E}^{l}$
			CH <sub>3</sub> SnH <sub>3</sub>		$2.143 \pm 0.002$	M <sup>k</sup>
			(CH <sub>3</sub> ) <sub>3</sub> SnCl		$2.19 \pm 0.03$	$\mathbf{E}'_{\mathbf{E}'}$
			CH <sub>3</sub> SnBr <sub>3</sub>		$\sim 2.17$	$\mathbf{E}^{t}$
C-I	2 10	9 114	(CH <sub>2</sub> ) <sub>2</sub> ShBr		$2.17 \pm 0.05$ 2.12 $\pm 0.02$	E E <sup>l</sup>
	2.10	4,114	~14		$2.12 \pm 0.02$ $2.15 \pm 0.02$	$\mathbf{E}^{l}$
			CHI3	2.14	$2.12 \pm 0.02$	$\mathbf{E}^{l}$
			$CH_2I_2$	2.15	$2.12 \pm 0.04$	$\mathbf{E}^{l}$
			CH₃I	2.14	2.132	$\mathbf{M}^{ab}$
			0.0.1		2.1392	$M^{ac}$
NL NI	1 40	1 407	CF3I N.H.	1 40	$2.14 \pm 0.02$ 1 47 ± 0.02	$\mathbf{M}^{v}$ $\mathbf{F}^{l}$
1N1N	1.40	1,48/	1N2114	1.48	$1.47 \pm 0.02$ 1 46 $\pm 0.02$	E XC <sup>ag</sup>
			(CH <sub>2</sub> ) <sub>2</sub> N <sub>2</sub> H <sub>2</sub>		$1.45 \pm 0.02$	$E^{l}$
			N <sub>4</sub> S <sub>4</sub>		1.47	$\mathbf{E}^{l}$
N-O	1.36	1.458	NH <sub>2</sub> OH		1.46	$S^{ah}$
N-F	1.34	1.377	NF:	1.356	$1.37 \pm 0.02$	$\mathbf{E}^{l}$

			TABLE II (Conta	inued)		
Bond	rAB calcd. from normal valence radii <sup>6</sup>	$r_{AB}$ calcd. from $D_{np,A}$ and $x_{A}^{17}$	Molecule or crystal	$r_{AB}$ calcd. from exp. $D_{AB}$ <sup>17</sup>	rAB (exp.)	Source of rAB (exp.) <sup>a</sup>
					1.371	$\mathbf{M}^{ai}$
N-S	1.74	1.750	$N_4S_4$		1.74	$\mathbf{E}_{,}^{l}$
					$1.62 \pm 0.02$	E,
N-Cl	1.69	1.732	NCl <sub>3</sub>	1.77	1 70	0ª j
			CH NCI		1.70 $1.74 \pm 0.09$	ວ. <sub>E</sub> l
			(CH) NC1		$1.74 \pm 0.02$ 1.77 $\pm 0.02$	E E <sup>l</sup>
00	1 39	1 474	H <sub>2</sub> O.	1 470	$1.77 \pm 0.02$ $1.47 \pm 0.02$	E F <sup>l</sup>
0.0	ست.∢∙. ر	1.777	11,04	1.778	$1.47 \pm 0.02$ $1.49 \pm 0.02$	X Cak
					$1.49 \pm 0.02$ 1.48	S
0-F	1.30	1 436	0E4	1 403	$1.41 \pm 0.05$	$\mathbf{E}^{l}$
01	1.000	1.100	···		$1.38 \pm 0.03$	$S^{al}$
			NO <sub>3</sub> F		$1.42 \pm 0.05$	$\tilde{\mathbf{E}}^{l}$
O-Si	1.83	1.688	$SiO_2$	1.68	1.61	$\mathbf{XC}^m$
			Si(OCH <sub>3</sub> ) <sub>4</sub>		$1.64 \pm 0.003$	$E^{am}$
			(CH <sub>3</sub> ) <sub>6</sub> Si <sub>3</sub> O <sub>3</sub>		$1.66 \pm 0.04$	$\mathbf{E}^{an}$
			(CH <sub>3</sub> ) <sub>3</sub> SiOSi(CH <sub>3</sub> ) <sub>3</sub>		$1.63 \pm 0.03$	$\mathbf{E}^{am}$
			Cl <sub>3</sub> SiOSiCl <sub>3</sub>		$1.64 \pm 0.05$	$E^{am}$
0-P	1.76	1.688	$P_4O_6$		$1.67 \pm 0.03$	$\mathbf{E}^{l}$
					$1.65 \pm 0.02$	$\mathrm{E}^{l}$
					1.63	S°°
0 <b>-</b> ℃1	1.65	1.716	$Cl_2O$	1.713	$1.68 \pm 0.03$	$\mathbf{E}^{t}$
					$1.701 \pm 0.020$	$\mathbf{E}^{ap}_{,}$
O-As	1.87	1.795	$As_4O_6$	1.816	$1.80 \pm 0.02$	$\mathbf{E}'_{\mathbf{J}}$
			<b>6</b> 4 -		$1.78 \pm 0.02$	E'
O-Sb	2.07	1.992	$Sb_4O_6$	1.996	$2.0 \pm 0.1$	XC <sup>a</sup>
			$Sb_2O_3$	1 (00	2.00	XC <sup>a</sup>
F-F	1.28	1.442	$F_2$	1.438	$1.435 \pm 0.01$	$E^*$
F-S1	1.81	1.014	SIF <sub>4</sub>	1.014	$1.54 \pm 0.02$	E Nas
			SIHF3 SILE		$1.501 \pm 0.005$	M <sup></sup>
			SIH3F SICID		$1.593 \pm 0.002$	IVI Mas
			SICIF3 SiD_F		$1.000 \pm 0.005$ $1.500 \pm 0.005$	1V1 N # 48
E.D	1 74	1 619	DE		$1.500 \pm 0.005$ $1.52 \pm 0.04$	
r-r	1.74	1.012	L L 3		$1.52 \pm 0.04$ 1.535	Man
F-C1	1 63	1 661	CIF	1 661 or	1.6281	Mav
	1.00	1.001	Chr	1.657	1.0201	114
F-Ge	1 86	1 663	GeF	1.001	$1.67 \pm 0.03$	$\mathbf{E}^{aw}$
F-As	1.85	1.716	AsF <sub>3</sub>	1.717	$1.72 \pm 0.02$	$\mathbf{E}^{l}$
					$1.712 \pm 0.006$	$S^{ax}$
F–Br	1.76	1.774	BrF	1.778	1.759	$\mathbf{M}^{ay}$
F-Sb	2.05	1.912	$SbF_3$	1.923		
Si-Si	2.34	2.290	Si	2.29	2.352	XCaz
			$Si_2H_6$		$2.32 \pm 0.03$	$\mathbf{E}^{l}$
Si-S	2.21	2.136	SiS <sub>2</sub>	2.13	2.14	$\mathrm{XC}^m$
Si-C1	2.16	2.033	SiCL	2.032	$2.02 \pm 0.02$	$\mathbf{E}^{l}$
			SiHCl <sub>3</sub>		$1.98 \pm 0.02$	XG'
					$2.00 \pm 0.03$	E,
					$2.01 \pm 0.03$	$E'_{-'}$
			0.111 01		$2.05 \pm 0.03$	$E^{\prime}$
			$S_1H_2Cl_2$		$2.02 \pm 0.03$	E'
			SIH <sub>3</sub> CI		$2.00 \pm 0.00$	E Napa
					2.000 2.048 + 0.004	тл 101
			SICIE		1.989 + 0.004	M <sup>us</sup>
			SICIL'3		$2.03 \pm 0.03$	$\mathbf{E}^{l}$
			SiBrCl <sub>3</sub>		$2.05 \pm 0.05$	$\tilde{\mathbf{E}}^{l}$
Si-Br	2.31	2.197	SiBr₄	2.199	$2.14 \pm 0.02$	$\vec{\mathbf{E}}^{l}$
-	_ · • •				$2.15 \pm 0.02$	$\mathbf{E}^{l}$
			SiH₃Br		2.209	$\mathbf{M}^{bc}$
			SiBrF <sub>3</sub>		$2.153 \pm 0.018$	$M^{as}$
			$\mathrm{SiBr}_{2}\mathrm{F}_{2}$		$2.16 \pm 0.02$	$\mathbf{E}_{\mathbf{i}}^{l}$
Si-I	2.50	2.430	$SiI_4$	2.436	$2.43 \pm 0.02$	$\mathbf{E}^{\iota}$

			Table II	(Continued)		
Bond	r <sub>AB</sub> calcd. from normal valence radii <sup>6</sup>	$r_{AB}$ calcd. from $D_{np,A}$ and $x_A^{17}$	Molecule or crystal	$r_{AB}$ calcd. from exp. $D_{AB}$ <sup>17</sup>	rAB (exp.)	Source of r <sub>AB</sub> (exp.) <sup>a</sup>
P-P	2.20	2,210	Normal $P_4$	2.205	$2.21 \pm 0.02$	$\mathbf{E}^{l}$
		0.101	P (black)		2.17-2.20	XC
P-S	2.14	2.121	$P_4S_3$	0.000	2.15	$\mathbf{E}^{i}$
P-CI	2.09	2.027	PCI <sub>3</sub>	2.023	$2.00 \pm 0.02$	E' D'
					$2.03 \pm 0.02$	E'
	2.24	0.404		0.100	$2.043 \pm 0.003$	M <sup>oo</sup>
P-Br	2.24	2.191	$PBr_3$	2.188	$2.23 \pm 0.01$	E'
	0.40	0. (00)	D.I.	0.415	$2.18 \pm 0.03$	E'
P-1	2.43	2.420	$\mathbf{P1}_3$	2.415	$2.52 \pm 0.01$	E' D <sup>l</sup>
					2.40	E' E'
C C	2 08	9.070	c	9.059	$2.43 \pm 0.04$	E
6-6	4.08	2.070	08 8.	2.000	$2.07 \pm 0.02$	E <sup>1</sup>
			178	2.000	$2.07 \pm 0.02$	
			н.с.		$2.03 \pm 0.02$ $2.05 \pm 0.02$	
			5.C1.		$2.00 \pm 0.02$ 2.04 $\pm 0.05$	$\mathbf{F}^{l}$
			02012		$2.04 \pm 0.00$	$\mathbf{E}^{l}$
					$2.00 \pm 0.00$ 2.07 ± 0.10	$\mathbf{E}^{l}$
S-C1	2 03	2 007	SCI		$1.99 \pm 0.03$	$\mathbf{E}^{l}$
5 61	2.00	2:001	5012		$2.00 \pm 0.02$	$\mathbf{E}^{l}$
			S-Cl	2.015	$1.98 \pm 0.05$	$\mathbf{E}^{l}$
			0.012	,	$1.99 \pm 0.03$	$\overline{\mathbf{E}}^{l}$
					$2.01 \pm 0.07$	$\overline{\mathbf{E}}^{l}$
S-As	2.25	2.241	As <sub>4</sub> S <sub>4</sub>	2.230	$2.23 \pm 0.02$	$\overline{\mathbf{E}}^{l}$
10			•		2.19 - 2.27	XC <sup>be</sup>
			As <sub>4</sub> S <sub>6</sub>	2,230	$2.25 \pm 0.02$	$\mathbf{E}^{l}$
S-Br	2.18	2.167	$S_2Br_2$	2.156		
C1-C1	1.98	1.998	$Cl_2$	1.998	1.988	S <sup>bf</sup>
Cl-Ge	2.21	2.085	GeCl₄	2.097	$2.08 \pm 0.03$	$\mathbf{E}^{l}$
			GeH₃C1		$2.147 \pm 0.005$	$\mathbf{M}^{i}$
C1-As	2.20	2.137	AsCl <sub>3</sub>	2.138	$2.16 \pm 0.03$	$\mathbf{E}^{l}$
					$2.17\pm0.02$	$\mathbf{E}^{l}$
					$2.161 \pm 0.004$	$\mathbf{M}^{bd}$
			$(CH_3)_2AsCl$		$2.18 \pm 0.04$	$\mathbf{E}^{l}$
C1-Se	2.16	2.137	SeC1 <sub>2</sub> ·	2.138		
C1–Br	2.13	2.138	BrCl	2.141	2.138	Mog
C1–Sn	2.39	2.283	SnCl <sub>4</sub>	2.296	$2.30 \pm 0.03$	E,
			CH <sub>3</sub> SnCl <sub>3</sub>		$2.32 \pm 0.03$	$\mathbf{E}_{-}^{*}$
			$(CH_3)_2SnCl_2$		$2.34 \pm 0.03$	$\mathbf{E}^{i}$
	- ···		(CH₃)₃SnCl	<b>a</b> aa <i>i</i>	$2.37 \pm 0.03$	$E'_{-'}$
Cl-Sb	2.40	2.336	SbCl <sub>3</sub>	2.334	$2.37 \pm 0.02$	E'
Cl-Te	2.36	2.331	TeCl <sub>2</sub>	0.010	$2.36 \pm 0.03$	E' D'
CI-I	2.32	2.313	ICI	2.319	$2.30 \pm 0.03$	E.
0.0.	0.44	0 410	<b>C</b> -	9 400	2.324	S. •
GeGe	2.44	2.419	Ge	2,408	2.400	$\Sigma^{l}$
0. D.	0.00	9.050	$Ge_2\Pi_6$		$2.41 \pm 0.02$	$\mathbf{E}$
Ge-Dr	2.30	4,202	Geb14		2.02 0.94	
					$2.0 \pm 0.02$	$\mathbf{E}^{l}$
Carl	9 55	2 100	Cel	2 470	2.23 ± 0.02 9.47	$\mathbf{F}^{l}$
06-1	2.00	2.400	0014	2.10	2.48	E,
					2.10 2.50 ± 0.03	Ē'
As-As	2 42	2 470	Normal As	2.470	$2.44 \pm 0.03$	ਸ ਸ
As-Br	$\frac{2.35}{2.35}$	2.306	AsBr <sub>3</sub>	2.308	$2.36 \pm 0.02$	۔ ١٤′
			-		2.31	$\mathbf{E}^{l}$
					$\cdot 2.33 \pm 0.02$	$\mathbf{E}'$
			(CH <sub>3</sub> ) <sub>2</sub> AsBr		$2.34 \pm 0.04$	$\mathbf{E}'$
As-I	2.54	2.543	$AsI_3$	2.547	$2.58 \pm 0.01$	$\mathbf{E}_{\mathbf{I}}^{l}$
				•	2.51	$\mathbf{E}_{.}^{\prime}$
					2.541	E'
			(OT ) 1 -		$2.55 \pm 0.03$	E'
	0.04	0.040	(CH <sub>3</sub> ) <sub>2</sub> AsI		$2.52 \pm 0.03$	E <b>F</b>
Se-Se	2.34	2.348	Se6		2.32	E.

			TABLE II (Con	utinued)		
Bond	rAB calcd. from normal valence radii <sup>6</sup>	$r_{AB}$ calcd. from $D_{np,A}$ and $x_A^{17}$	Molecule or crystal	$r_{AB}$ calcd. from exp. $D_{AB}$ <sup>17</sup>	rAB (exp.)	Source of rAB (exp.) <sup>a</sup>
			Se <sub>8</sub>		$2.34 \pm 0.02$	$XC^{bh}$
			Se (gray)	2.32	2.32	XC <sup>m</sup>
Br–Br	2.28	2.289	$Br_2$	2.288	$2.28 \pm 0.02$	$\mathbf{E}^{l}$
					2.279	$\mathbf{E}^{l}$
					2.286	S <sup>h</sup>
Br–Sn	2.54	2.452	$\operatorname{SnBr}_4$	2.454	$2.44 \pm 0.02$	$\mathbf{E}^{l}$
			CH <sub>3</sub> SnBr <sub>3</sub>		$2.45 \pm 0.02$	$\mathbf{E}^{l}$
			$(CH_3)_2SnBr_3$		$2.48 \pm 0.02$	E'
			(CH <sub>3</sub> ) <sub>3</sub> SnBr		$2.49 \pm 0.03$	$\mathbf{E}^{l}$
Br–Sb	2.55	2.506	SbBr <sub>1</sub>	2.473	$2.52 \pm 0.02$	$\mathbf{E}^{i}$
					2.47	$\mathbf{E}^{l}$
					$2.51 \pm 0.02$	$\mathbf{E}^{l}$
Br–Te	2.51	2.502	$TeBr_2$		$2.49 \pm 0.03$	$\mathbf{E}^{l}$
					$2.51 \pm 0.02$	$\mathbf{E}^{l}$
Br–I	2.47	2.478	IBr	2.476		
Sn-Sn	2.80	2.834	Sn (gray)	2.824	2.80	XC <sup>m</sup>
Sn-I	2.73	2.694	$SnI_4$		$2.64 \pm 0.04$	$\mathbf{E}^{l}$
					2.63	XC <sup>m</sup>
			CH <sub>8</sub> SnI <sub>3</sub>		$2.68 \pm 0.02$	$\mathbf{E}^{l}$
			$(CH_3)_2SnI_2$		$2.69 \pm 0.03$	$\mathbf{E}^{l}$
			(CH <sub>3</sub> ) <sub>3</sub> SnI		$2.72 \pm 0.03$	$\mathbf{E}^{l}$
Sb-Sb	2.82	2.894	Normal Sb (cr)	2.888	2.87	$XC^m$
Sb-I	2.74	2.747	$SbI_3$	2.738	$2.75 \pm 0.02$	$\mathbf{E}^{l}$
					2.74	$\mathbf{E}^{l}$
					$2.67 \pm 0.03$	$\mathbf{E}^{l}$
Te-Te	2.74	2.814	Te (cr)		2.86	$\mathbf{XC}^{m}$
I–I	2.66	2.694	I <sub>2</sub>	2,681	$2.66 \pm 0.01$	$\mathbf{E}^{l}$
					2.674	$\mathbf{E}^{l}$
					2.662	S <sup>bi</sup>
					2 70	$XC^{m}$

2.662 S<sup>44</sup>
 2.70 XC<sup>m</sup>
 \* S = from spectroscopic data, usually infrared; M = from microwave data; E = from electron diffraction data from gas, XC = from X-ray diffraction data from gas. <sup>4</sup> H. Sponer, 'Molexilispektren, I,'' I. Springer, Berlin, 1935. c G. Herzberg, 'Infrared and Raman Spectra of Polyatomic Molecules,'' D. Van Nostrand Co., New York, N. V., 1945. <sup>4</sup> G. E. Hansen and D. M. Dennison, J. Chem. Phys. 20, 739 (1952).
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The general degree of agreement between experiquite insensitive to the choice of a, within this mental and calculated interatomic distances is range. The constant energy radii and calculated interatomic distances given here are all for a value of

$$a = 4.605 \times 10^8 \,\mathrm{cm}^{-1}$$
 (14)

This choice has the advantage of yielding the simple relationship

$$r_{\rm AB} = r_{\rm A}^* + r_{\rm B}^* - \frac{1}{2} \log D_{\rm AB}$$
(15)

when the values of  $r_{AB}$ ,  $r_A^*$  and  $r_B^*$  are in Å. and those of  $D_{AB}$  are in kcal./mole.

## Comparison with Experiment

With the aid of this equation, the constant energy radii listed in Table I have been obtained. These, in turn, have been used to compute the values of  $r_{AB}$  (calcd.) listed and compared with the corresponding experimental values in Table II.

Calculations have been made both from the experimental bond energies and from bond energies computed from electronegativities and non-polar bond-energy contributions. Both of these are given in the preceding paper.<sup>17</sup>

The average differences between the observed and computed distances are about 0.019 Å. for the figures from experimental bond energies and about 0.024 Å. for those from computed bond energies. These averages would be reduced somewhat if one omitted those cases in which, from other considerations, there is reason to believe that the experimental values of the bond energy (e.g., H-As) or the bond length (e.g., H-Se or Te-Te) are quite inaccurate.

In order to obtain even rough agreement for the hydrogen compounds, it was found necessary to use several different values of  $r_{\rm H}^*$ , depending on the row of the Periodic Table in which the element to which the hydrogen is bonded belongs. This is probably a result of the fact, already noted,<sup>15</sup> that these bonds do not obey the assumed energydistance relationship well, at least with the same value of *a* which is found satisfactory for other bonds. An alternative explanation is that equation (11) does not hold with sufficient accuracy for

(17) M. L. Huggins, THIS JOURNAL, 75, 4122 (1953).

bonds involving hydrogen, with the same value of  $E^*_{rep}$  as is satisfactory for other bonds.

It will be noted that the discrepancies in the cases of such very strong, very polar bonds as Si–O and Si–F have been greatly reduced, but not entirely eliminated. (A different assumption as to the sublimation energy of silicon does not improve the situation appreciably.) It seems likely that here, as with bonds involving hydrogen, the basic assumptions underlying the present treatment no longer hold with sufficient accuracy. One way out of the difficulty would be to add to equation (15) another term, involving either the electronegativity or perhaps the fraction of double-bond character, but this does not seem warranted in the present state of our knowledge.

Instead of using Equation (15), one can obviously compute interatomic distances from the non-polar radii by means of the relation

$$r_{AB} = r_{np,A} + r_{np,B} - 1/2 \log \left( \frac{D_{AB}}{D_{np,A} + D_{np,B}} \right)$$
 (16)

making use of the non-polar bond-energy contributions listed in the preceding paper. A set of non-polar radii, consistent with the constant energy radii and the non-polar bond-energy contributions which have been listed, is included in Table I. The differences between these and the corresponding radii given by Schomaker and Stevenson are slight. Differences between interatomic distances calculated by equation (16) and those calculated by equation (15) are only such as result from rounding off of the atomic constants used.

In summary, the results presented show that interatomic distances for single bonds between atoms exhibiting their normal valences can be computed, at least within about 0.02 Å., from experimental or calculated bond energies by means of equation (15) or (16), and the constant energy radii of Table I.

ROCHESTER, N. Y.

[CONTRIBUTION FROM THE MASS SPECTROSCOPY LABORATORY, HOWARD UNIVERSITY]

# Electron Impact Studies in CH<sub>4</sub>, CH<sub>3</sub>Cl, CH<sub>3</sub>Br and CH<sub>3</sub>I

By Herman Branson and Carter Smith

RECEIVED MARCH 27, 1953

Data on the appearance potentials of the positive ions produced on electron impact with CH<sub>4</sub>, CH<sub>3</sub>Cl, CH<sub>3</sub>Br and CH<sub>3</sub>I in a 60° Nier type mass spectrometer are used to calculate the heat of sublimation of carbon,  $L(C) \leq 5.90$  e.v. Further calculations from the data give D(C-H) = 3.5 e.v.,  $D(C-2H) \leq 7.4$  e.v.,  $D(C-3H) \geq 11.2$  e.v.,  $D(CH_3-H) \leq 4.2$  e.v.,  $D(CH_3-CI) \leq 3.4$  e.v.,  $D(CH_3-Br) \leq 3.1$  e.v., and  $D(CH_3-I) \leq 2.3$  e.v. The measured ionization potentials are  $I(CH_4^+) = 13.1$  e.v.,  $I(CH_3CI^+) = 11.3$  e.v.,  $I(CH_3CI^+) = 10.5$  e.v., and  $I(CH_3I^+) = 9.6$  e.v. The derived  $I(CH_2^+)$  is  $\leq 12$  v.

In the mass spectrometer ions are formed by collisions of electrons with molecules and separated according to their mass to charge ratio, following the relation  $m/q = r^2B^2/2V$  where r is the radius of the ion path in meters, B is the magnetic induction in webers per meter<sup>2</sup>, V is the ion accelerating voltage in volts, m is the mass of the ion in kilograms, and q is the charge on the ion in coulombs. One can measure in the ion gun the appearance potential or the minimum energy required to pro-

duce a particular ion. The appearance potential of undissociated ions often check and supplement spectroscopic data. For many substances the data are unique. The ionization potentials of radicals and the bond energies which may be computed provide valuable knowledge toward the understanding of molecular structure.

Electron impact studies in tri and higher atomic gases are complicated by a lack of information concerning the identities of the fragments pro-